than when the concentrations are the same with respect to numbers of grams.
5. Heydweiller's relationship, connecting the surface tension of solutions with the number of equivalents present and the ionization of the substance, was found to fail with our results in the case of calcium chloride, but at times to show up remarkably well with both zinc nitrate and sodium chromate.
laboratory of Physical Chymbtry.
[Contribetions from the Chemical Laboratories of Columbia University, No. 223.]

## THE WEIGHT OF A FALLING DROP AND THE LAWS OF TATE, XVIII. THE DROP WEIGHTS, SURTACE TENSIONS AND CAPLLLARY CONSTANTS OF AQUEOUS SOLUTIONS OF ETHYL, METHYL AND AMYI ALCOHOLS, AND OF ACETIC AND FORMIC ACID. ${ }^{1}$

By J. Livingston R. Morgan and Maris Nembe. Received July 28. 1913.
In a previous paper ${ }^{2}$ it was shown that when the two non-associated liquids, benzene and carbon tetrachloride, were mixed together in equal parts by weight a critical temperature could be calculated for the mixture from the drop weight or surface tension, which was practically the mean of those of the two individual constituents; the only assumption made being that the density of the mixture is the mean of those of the two individual constituents. This can be shown in a more striking and direct way, and without any assumption at all, by calculating for each individual liquid an equation expressing the change of its surface tension, which is determined directly from drop weight, with the temperature, and taking the mean of the two. If the surface tension of the mixture, $\mathrm{I}: \mathrm{I}$, is then an additive property, this will be the equation giving its change with temperature. As Morgan and Thomssen worked at only one temperature, this calculated equation cannot be compared directly with an experimental one for the mixture; but a value from it can be calculated and then compared with the one value experimentally determined by them for the mixture. Proceeding in this way, we find that their results for the surface tensions of benzene and of carbon tetrachloride can be expressed by the equations $\gamma_{\mathrm{CHH}_{\mathrm{o}}}=30.498-0.1305 t$ and $\gamma_{\mathrm{CCh}}=28.129-$ $0.1156 t$, which, for a mixture of equal parts by weight would give $\gamma_{\text {mix. }}=$ 29.314 - $0.1231 t$, as the mean equation of change with the temperature.

At $23.6^{\circ}$, Morgan and Thomssen find $\gamma_{\text {mix. }}=26.382$, whereas the above formula leads to the result $\gamma_{\text {mix }}=26.409$; a difference of but 0.027 dynes, or 0.1\%.
${ }^{1}$ For other papers of this series, see reference on p. 182 I .
2 Morgan and Thomssen, This Journal, 33, 657-72 (i9ir).

That the surface tension of a mixture of non-associated liquids is an additive property has already been shown for this pair of liquids as well as for others, but in a less striking way. This is owing to the necessity, in the capillary rise method, of knowing the density of the mixture, or of assuming that neither liquid affects the other. ${ }^{1}$ We may conclude, then, that non-associated liquids, according to the definitions of either Ramsay and Shields, or Morgan, lead to systems, when mixed, whose surface tensions can be readily calculated by simply considering that property as an additive one.

The object of this investigation was to ascertain, by aid of the Morgan drop-weight apparatus, just how the surface tension of a mixture of two associated liquids is related, if at all, to the surface tensions of the constituents. For this purpose the drop weights were determined, and the surface tensions and capillary constants calculated. The following substances were examined: mixtures of methyl alcohol, ethyl alcohol, acetic acid and formic acid, each with water, in fourteen concentrations of each, ranging from $100 \%$ of water to $100 \%$ of the pure constituent -all at $30^{\circ}$; and solutions of amyl alcohol in six concentrations, at the same temperature (the slight solubility of amyl alcohol in water prevents the formation of homogeneous solutions of more than about $2.5 \%$ of amyl alcohol). In addition to these, the temperature coefficients of surface tension and of the capillary constant were determined from the results at three to four temperatures for certain aqueous solutions of methyl alcohol, ethyl alcohol, acetic acid and formic acid.
It is just in such cases as these that the drop-weight method shows its superiority over that depending upon capillary rise, as a means of finding the surface tension; for, as has been shown in previous papers, all influence of evaporation or any similar effect, can very readily be avoided in the drop-weight method, while it must always affect very considerably the results by capillary rise. This is especially true of solutions from which one constituent would evaporate, and thus cause a concentration change at the meniscus. The determination of the capillary rise of such liquids as we have studied would naturally be impossible in vacuo. The results of Ramsay and Aston on mixtures of pure organic liquids were possible by a method of this sort, only because they selected liquids which distilled nearly as chemical individuals, leaving a liquid behind of practically the same composition.
The ethyl alcohol used in this research was Kahlbaum's $99.8 \%$. Treating this with quicklime and distilling did not change the drop weight so that this original sample was used and considered as $100 \%$. It will be observed, from the table given later, that this $0.2 \%$ of water changed the surface tension of the alcohol only a few hundredths of one per cent. This probably is below the experimental error, and laborious attempts

[^0]to remove the final traces of water were, therefore, considered unnecessary. The methyl alcohol and amyl alcohol were specially prepared for us by the Hoffman and Kropff Chemical Company. The Kahlbaum acetic acid was purified by the freezing-out method until the drop weight remained constant. The formic acid ${ }^{1}$ was prepared by the Hoffman and Kropff Chemical Company, and further purified before use by several distillations under reduced pressure. All solutions were made up by weight.

Two tips were used in the course of the work. Their constants were found in the usual way by aid of benzene ${ }^{2}$ and were later verified against water, the calculated surface tension being compared with the surface tension of water from the equation of change with the temperature given by Morgan and McAfee. ${ }^{3}$ At $40^{\circ}$, Tip No. I gave an average drop weight of benzene of 27.592 milligrams, which leads to $K_{\mathrm{B}}=\mathbf{2} .3012$. Tip No. 2 at $30^{\circ}$ gave a drop weight for benzene of 28.912 milligrams, leading to $K_{\mathrm{B}}=2.2954$.

To calculate the surface tension in dynes per centimeter ( $\gamma$ ) from the drop weight in milligrams, and the capillary constant ( $a^{2}$ ) from the drop volume in milli-cubic centimeters ( $w / d$ ), we have now the equations: $\gamma=0.9190 \times w_{1} ; a^{2}=0.1876 \times w_{1} / d ;$ and $\gamma=0.9213 \times w_{2} ; a^{2}=0.188 \mathrm{I} \times$ $w_{2} / d$.

By aid of these $\gamma$ relations, it is now possible to verify the standardizations of the tips, for surface tensions calculated from the drop weights of water should, if the constants $K_{\mathrm{B}}$ are correct, agree with the results of the Morgan-McAfee equation. Tip No. I, for example, leads from its drop weight of water by aid of the above equation to a surface tension at $40^{\circ}$ of 69.348 , which agrees within $0.03 \%$ with the calculated value. Tip No. 2 also led to satisfactory results in a similar way.

This verification was repeated from time to time during the work, that we might be certain that no accidental change had occurred in the size of the tips.

For the pure amyl alcohol and acetic acid, and for all solutions, the following modification of the usual method was adopted: The weighing vessel, containing some of the liquid was weighed with the stopper in, and then cooled by immersing it partly in cold water, to prevent any loss by evaporation when the stopper was removed to attach the vessel to its

[^1]plug. The whole apparatus was then placed in the constant temperature water bath and allowed to stand for from 20 to 30 minutes-and the desired number of drops allowed to form and fall very slowly. It is not necessary here to allow the first drop to hang for 5 minutes, as in the original method, for the vessel has already been saturated from the larger amount of liquid put in the weighing vessel, previous to setting up. Before removing the weighing vessel at the end of the experiment, naturally, it was again cooled, to prevent loss of vapor in removing the vessel from the apparatus and when inserting the stopper. The gain in weight was then the weight of the number of drops taken. In order to make sure that the liquid originally placed in the weighing vessel did not lose in weight while standing in the apparatus, several blanks were made. A typical blank was the following: A $75 \%$ solution of methyl alcohol in water was allowed to stand in the weighing vessel, while the whole apparatus remained for 50 minutes in the water bath at $60^{\circ}$ when the loss in weight was found to be but 0.4 milligram, 'which may be considered as negligible, in comparison with the weight of the 20 to 30 drops used in the determination.

The great advantage of this method is that when the first drop of liquid is run over on the tip, and exposed to the air space of the weighing vessel, no change takes place in it, for that space is already saturated with just the vapor which it itself would produce-and the diop forms and falls, retaining throughout its original concentration.

In the following tables are grouped together the average values of the drop weights found, and those of the surface tension and capillary constant calculated, together with the other data necessary for the calculation:

Aqueous Solutions of Ethyl Alcohol at $30^{\circ} \mathrm{C}$.-Tip No. i.

| Wt. Per cent. | Density. ${ }^{\text {d }}$ | Grams per 100 cc . | Drop wt. | Surf. tens. | Cap. const. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 0.9958 | 0.000 | 77.290 | 71.030 | 14.564 |
| 0.979 | 0.9940 | 0.973 | 71.380 | 65.600 | 13.472 |
| 2.143 | 0.9918 | 2.125 | 66.210 | 60.847 | 12.524 |
| 4.994 | 0.9868 | 4.928 | 57.820 | 53.137 | 10.992 |
| 10.385 | 0.9783 | IO. 156 | 48.605 | 44.668 | 9.32 I |
| 17.979 | 0.9671 | 17.39 | 40.600 | 37.311 | 7.876 |
| 25.00 | 0.9563 | 23.91 | 35.843 | 32.94 I | 7.031 |
| 29.98 | 0.9476 | 28.41 | 33.534 | 30.818 | 6.639 |
| 34.89 | 0.9383 | 32.74 | 31.879 | 29.297 | 6.374 |
| 50.00 | 0.9058 | 45.29 | 28.859 | 26.52 I | 5.977 |
| 60.04 | 0.8830 | 53.01 | 27.587 | 25.352 | 5.86I |
| 71.85 | 0.8547 | 61.44 | 26.331 | 24.198 | 5.779 |
| 75.06 | 0.8470 | 63.58 | 25.952 | 23.850 | 5.748 |
| 84.57 | 0.8212 | 69.45 | 24.824 | 22.813 | 5.671 |
| $95 \cdot 57$ | 0.7939 | 75.88 | 23.230 | 21.348 | $5 \cdot 489$ |
| 100.00 | 0.7810 | 78.10 | 22.585 | 20.756 | 5.425 |

Agueots Solutions of Methyl Alcohol at $30^{\circ} \mathrm{C}$.-Tip No, 2. Wt. Per cent. Density. Grams per 100 cc . Drop wt. Surf. tens. Cap. const.

| 0.000 | $0.9958^{1}$ | 0.000 | $77.290^{2}$ | 71.030 | 14.564 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.01 I | 0.9939 | 1.005 | 73.940 | 68.120 | 13.993 |
| 2.500 | 0.9912 | 2.478 | 70.384 | 64.845 | 13.357 |
| 4.997 | 0.9867 | 4.93 I | 65.444 | 60.294 | 12.476 |
| 9.994 | 0.9781 | 9.775 | 58.245 | 53.661 | 1 I .201 |
| 15.00 | 0.9703 | 14.55 | 52.987 | 48.817 | 10.272 |
| 20.00 | 0.9628 | 19.26 | 48.729 | 44.894 | 9.520 |
| 25.00 | 0.9549 | 23.87 | 45.380 | 41.809 | 8.939 |
| 29.98 | 0.9473 | 28.40 | 42.409 | 39.071 | 8.604 |
| 39.98 | 0.9289 | 37.14 | 37.920 | 34.936 | 7.679 |
| 50.00 | 0.9091 | 45.46 | 34.563 | 31.843 | 7.151 |
| 60.00 | 0.8876 | 53.26 | 31.880 | 29.371 | 6.756 |
| 70.00 | 0.8637 | 60.46 | 29.533 | 27.209 | 6.432 |
| 75.00 | 0.8514 | 63.86 | 28.409 | 26.173 | 6.276 |
| 80.03 | 0.8384 | 67.10 | 27.303 | 25.154 | 6.126 |
| 90.01 | 0.8114 | 73.04 | 25.073 | 23.100 | 5.813 |
| 100.00 | 0.7825 | 78.25 | 22.834 | 21.037 | 5.489 |

Aqueous Soluttons of Amye Alcohol at $30^{\circ} \mathrm{C}$.-Tip No. 2.

| 0.000 | $0.998^{8}$ | 0.000 | $77.290^{2}$ | 71.030 | I4.564 |
| :---: | :---: | :---: | :---: | :---: | ---: |
| 0.250 | 0.9954 | 0.249 | 58.300 | 53.712 | II.017 |
| 0.500 | 0.9950 | 0.498 | 50.100 | 46.157 | 9.47 I |
| 0.750 | 0.9946 | 0.746 | 44.769 | 41.247 | 8.467 |
| 1.000 | $0.994^{2}$ | 0.994 | 40.845 | 37.63 I | 7.728 |
| 1.500 | 0.9934 | 1.490 | 35.280 | 32.504 | 6.680 |
| 2.000 | 0.9926 | 1.985 | 31.116 | 28.667 | 5.897 |
| 2.498 | 0.992 I | 2.478 | 27.924 | 25.726 | 5.294 |
| 100.000 | $\ldots$ | $\ldots$ | 24.200 | 22.296 | $\cdots$. |

Agueous Solutions of Acetic Acid at $30^{\circ}$.-Tip No. i.

| 0.000 | $0.9958^{4}$ | 0.000 | 77.290 | 71.030 | 14.564 |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 1.000 | 0.9972 | 0.997 | $73.544^{\text {b }}$ | 67.756 | 13.873 |
| 2.475 | 0.9979 | 2.470 | $69.46^{5}$ | 63.995 | 13.093 |
| 5.001 | 1.0025 | 5.014 | $64.51^{5} 2^{5}$ | 59.435 | 12.104 |
| 10.01 | 1.0090 | 10.100 | 58.215 | 53.500 | 10.824 |
| 14.98 | 1.0152 | 15.21 | $53.655^{5}$ | 49.451 | 9.945 |
| 20.09 | 1.0212 | 20.52 | 50.550 | 46.455 | 9.286 |
| 30.09 | 1.0322 | 31.06 | 45.995 | 42.269 | 8.360 |
| 40.11 | 1.0417 | 41.78 | 42.844 | 39.374 | 7.716 |
| 49.96 | 1.0494 | 52.43 | 40.380 | 37.109 | 7.219 |
| 60.05 | 1.0554 | 63.38 | 38.123 | 35.035 | 6.777 |
| 69.91 | 1.0591 | 74.04 | 36.016 | 33.099 | 6.380 |
| 79.88 | 1.0599 | 84.67 | 33.761 | 31.026 | 5.976 |
| 90.04 | 1.0554 | 95.03 | 30.205 | 28.677 | 5.547 |
| 100.00 | 1.0384 | 103.84 | 27.992 | 25.725 | 5.057 |

${ }^{1}$ Extrapolated from the same source.
${ }^{2}$ Tip No. 1 .
${ }^{3}$ Densities from the "Tabellen" on the assumption that equal concentrations lowered the density of water at $30^{\circ}$ by the same amount as at $20^{\circ}$.
${ }^{4}$ Densities from the "Tabellen."
${ }^{5}$ Tip No. 2.

Aqueous Solutions of Formic Acid at $30^{\circ} \mathrm{C}$ - -Tip No. 2.

| Wt. Per cent. | Density. ${ }^{1}$ | Gm. per 100 cc. | Drop wt. | Suri. tens. | Cap. const |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 0.9958 | 0.0000 | $77.290^{1}$ | 71.030 | 14.564 |
| 1.000 | 0.9995 | 0.9995 | 75.780 | 69.816 | 14.26 I |
| 2.500 | I. 0029 | 2.573 | 73.835 | 68.024 | 13.848 |
| 5.000 | 1.0090 | 5.045 | 71.319 | 65.706 | 13.295 |
| 10.00 | I. 0198 | 10.198 | 67.362 | 62.06 I | 12.425 |
| 15.00 | I. 0309 | 15.46 | 64.252 | 59.197 | 11.724 |
| 20.00 | I. 0423 | 20.85 | 61.779 | 56.917 | 11.149 |
| 25.00 | I. 0538 | 26.37 | 59.904 | 55.190 | 10.693 |
| 30.01 | I 06653 | 31.97 | 58.152 | 53.575 | 10.268 |
| 40.00 | I.0881 | 43.52 | 54.992 | 50.664 | 9.507 |
| 50.00 | I. 1113 | 55.57 | 52.222 | 48.112 | 8.839 |
| 60.00 | I. 1326 | 67.96 | 49.637 | 45.731 | 8.244 |
| 70.00 | I. 1544 | 80.81 | 46.934 | 43.240 | 7.648 |
| 75.00 | I. 1651 | 87.38 | 45.577 | 41.990 | 7.358 |
| 80.01 | I. 1743 | 93.96 | 44.180 | 40.703 | 7.077 |
| 90.00 | I. 1942 | 107.48 | 41.274 | 38.026 | 6.501 |
| 100.00 | I. 2089 | 120.89 | 38.295 | 35.28 I | 5.959 |

In the following tables are given the results for the solutions we have studied, at the various temperatures employed. Here, after the drop weights had been determined, the equations for their variation with the temperature were found, by the aid of the method of least squares, and these equations transformed, by multiplying each term by the proper constant for the tip, into equations giving the variation of the surface tension in dynes with the temperature. And the same transformation was made with the equations representing the change in the drop volume (drop weight/density) with the temperature. From them, therefore, could be found the value of the capillary constant ( $a^{2}$, the height of ascension in a capillary tube with a bore radius of I millimeter, under ideal conditions) at any desired temperature. In order to save space the results and equations for the drop weight and the drop volume are omitted, only the derived values and equations being given.

| Aqueous Solutions of Ethyl Alcohol. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $25 \%$ Av. Mol. Wt. $=2 \mathrm{I} .25$. |  |  |  |  | $50 \%$ Av. Mol. Wt. $=25.90$. |  |  |
| $t$. | d. | $\gamma$. | $a^{2}$. | $t$. | d. | r. | $a^{\text {a }}$ |
| $\bigcirc$ | 0.9712 | 36.455 | 7.664 | $\bigcirc$ | 0.9294 | 28.391 | 6.237 |
| 10 | 0.9667 | 35.186 | 7.429 | 10 | 0.9218 | 27.768 | 6.150 |
| 20 | 0.9619 | 34.014 | 7.218 | 20 | 0.9140 | 27.145 | 6.064 |
| 30 | 0.9563 | 32.940 | 7.031 | 30 | 0.9058 | 26.522 | 5.978 |
| $\begin{array}{ll} \gamma t=36.455-0.1318 t+0.000486 t^{2} & \gamma t=28.39 \mathrm{I}-0.0623 t \\ a_{t}{ }^{2}=7.644-0.0247 t+0.00012 t^{2} & a_{t}{ }^{2}=6.237-0.0086 t \end{array}$ |  |  |  | $\begin{aligned} \gamma t & =28.39 \mathrm{I}-0.0623 t \\ a_{l}{ }^{2} & =6.237-0.0086 t \end{aligned}$ |  |  |  |
|  |  |  |  |  |  |  |  |

${ }^{1}$ The densities here were interpolated from the results of Drucker (Ann. d. Phys., 28,$217 ; 38$, IOI8) who gives them at $25^{\circ}$ based on water at $25^{\circ}$ and at $35^{\circ}$ based on water at $35^{\circ}$. The mean of the two values was taken as equal to density at $30^{\circ}$, based on water at $30^{\circ}$; and this was recalculated so as to be based on water at $4^{\circ}$.

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Aqueous Solutions Ethyl Alcohol (Continued).
$75 \% \mathrm{Av} . \mathrm{Mol} . \mathrm{Wt}=33.13$.

| 6 | $d$ | $\ddots$ | $d^{2}$ |
| :---: | :---: | :---: | :---: |
| 0 | 0.8725 | 26.157 | $6.12 I$ |
| 10 | 0.8643 | 25.406 | 6.002 |
| 20 | $0.855^{2}$ | 24.654 | 5.882 |
| 30 | 0.8472 | 23.903 | 5.761 |

$\gamma_{t}=26.157-0.0752 t$
$a_{i}^{2}=6.12 \mathrm{I}-0.0120 t$

| b. | d. | $\gamma$ | $a^{2}$. |
| :---: | :---: | :---: | :---: |
| $\bigcirc$ | 0.8195 | 23.68 I | 5.900 |
| 10 | 0.81 I 3 | 22.915 | 5.767 |
| 20 | 0.8027 | 22.150 | 5.634 |
| 30 | 0.7939 | 2I. 384 | 5.499 |

$100 \% \mathrm{Mol} . \mathrm{Wt}=46.05$.

| $t$. | $d$. | $\%$ | $a$. |
| ---: | :---: | :---: | :---: |
| 0 | 0.8063 | 23.090 | 5.847 |
| 10 | 0.7979 | 22.312 | 5.709 |
| 20 | 0.7895 | 2 I .534 | 5.569 |
| 30 | 0.7810 | 20.756 | 5.426 |
|  | $\gamma t=23-090-0.0778 t$ |  |  |
|  | $a_{t}^{2}=5.847-0.0140 t$ |  |  |

Aqueous Solutions of Methyl Alcohol.

```
            \(25 \% \mathrm{Ar}\). Mol. Wt. \(=20.23\).
        t. \(\quad d . \quad\) r. \(\quad a^{2}\).
        \(\begin{array}{llll}\text { o } & 0.9667 & 44.818 & 9.466\end{array}\)
        \(\begin{array}{llll}\text { 10 } & 0.9633 & 43.807 & 9.285\end{array}\)
        \(\begin{array}{llll}20 & 0.9594 & 42.796 & 9.108\end{array}\)
        \(\begin{array}{llll}30 & 0.9549 & 41.785 & 8.934\end{array}\)
\(\gamma_{t}=44.8 \mathrm{I} 8-\mathrm{o}\) - 10 II It
\(a_{i}^{2}=9.466-0.0177 t\)
        \(75 \%\) Av. Mol. Wt. \(=26.87\).
        \(\begin{array}{lll}0.9594 & 42.796 & 9.108 \\ 0.9549 & 41.785 & 8.934\end{array}\)
\(\gamma t=28.618-0.0814 t\)
\(a^{2}=6.675-0.0133 t\)
```

        \(50 \% \mathrm{Av} . \mathrm{Mol} . \mathrm{Wt} .=23.05\).
    | $t$. | $d$. | $\gamma$. | $a^{2}$. |
| ---: | :---: | :---: | :---: |
| 0 | 0.9287 | 34.309 | 7.543. |
| 10 | 0.9222 | 33.406 | 7.4 I 4. |
| 20 | 0.9157 | 32.664 | 7.283. |
| 30 | 0.909 I | 31.84 I | 7.15 I. |

$\gamma_{t}=34.309-0.0823 t$

| 0 | 0.8753 | 28.618 | 6.675 | 0 | 0.8102 | 23.447 | 5.909. |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 10 | 0.8673 | 27.804 | 6.545 | 10 | 0.8010 | 22.650 | 5.773. |
| 20 | 0.8594 | 26.991 | 6.412 | 20 | $0.79 \times 8$ | 21.853 | 5.635. |
| 30 | 0.8514 | 26.177 | 6.278 | 30 | 0.7825 | 21.057 | 5.494. |

$\gamma t=23.447-0.0797 t$

Aqueous Solutions of Acetic Acid.

$50 \%$ Av. Mol. Wt. $=\mathbf{2 7 . 7 2}$.

| $t$. | $d$. | $\%$ | $a^{2}$. |
| :---: | :---: | :---: | :---: |
| 10 | 1.0654 | 38.684 | 7.413. |
| 20 | 1.0575 | 37.878 | 7.313. |
| 30 | 1.0494 | 37.07 I | 7.213. |
| 40 | 1.0410 | 36.265 | 7.113. |

$\gamma_{t}=39.49 \mathrm{I}-0.0807 t$
$\gamma_{t}=46-57 \mathrm{I}-0.0808 t$
$a_{t}^{2}=9.118-0.0112 t$
$75 \% \mathrm{Av} . \mathrm{Mol} . \mathrm{Wt} .=37.90$.
$a_{i}^{2}=7.513-0.010 t$
$100 \%$ Av. Mol. Wt. $=60.03$.

| 20 | I.0497 | 26.701 | 5.194 |
| :--- | :--- | :--- | :--- |
| 30 | 1.0384 | 25.733 | 5.060 |
| 40 | I.0273 | 24.764 | $4.922:$ |

$\gamma_{t}=34.722-0.0903 t$
$a_{t}^{2}=6.514-0.01 \mathrm{I} 7 t$

$$
\begin{aligned}
\gamma t & =28.639-0.0969 t \\
a_{t}^{2} & =5.466-0.0136 t
\end{aligned}
$$

Aqueous Solutions of Formic Acm.

| $25 \%$ Av. Mol. Wt. $=21.23$. |  |  |  |  | $50 \%$ Av. Mol. Wt. $=25.82$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | d. | $\gamma$. | $a^{2}$. | $t$. | d. | $\gamma$. | ${ }^{2}$. |
| 25 | 1. 0570 | 55.665 | $10.75{ }^{2}$ | 25 | I.1155 | 48.585 | 8.893 |
| 30 | I. 0538 | 55.186 | 10.692 | 30 | I.III3 | 48.101 | 8.837 |
| 35 | 1.0504 | 54.706 | 10.634 | 35 | 1.1070 | 47.618 | 8.782 |
| $\begin{aligned} r_{t} & =58 . \\ a_{i}^{2} & =1 \end{aligned}$ | -0.09 |  |  | $\gamma_{2}{ }^{2}=51.000-0.0967 t$ |  |  |  |


| $t$. | $\begin{gathered} 75 \% \mathrm{~A} \\ d . \end{gathered}$ | $\mathrm{Wt} .=$ | $a^{2}$. |
| :---: | :---: | :---: | :---: |
| 25 | I. 1702 | 42.494 | 7.414 |
| 30 | 1.1651 | 41.985 | 7.358 |
| 35 |  | 41.476 | 7.301 |
|  | $\begin{aligned} \gamma t & =45.038-0.01018 t \\ a_{t}^{2} & =7.697-0.0113 t \end{aligned}$ |  |  |

## Discussion of the Results.

The curves representing the change in surface tension (the directly determined factor in the drop-weight method, without any necessity of knowledge as to the density) with the percentage composition of the solution, are very much of the same type for all the five liquids studied above in this way. In all cases the first addition caused a very considerable drop in the surface tension. The drop in the surface tension of water caused by the addition of very small amounts of amyl alcohol, is especially striking, and immediately suggests itself as the basis of a very delicate method for estimation of the amount of that substance when it is alone present in water solution. Thus the presence in solution of even so small an amount as $0.25 \%$ changes the surface tension of water from 71.03 to 53.713 , or nearly $25 \%$ at $30^{\circ}$, while the following changes are observed for other concentrations: for $0.5 \%$, nearly $38 \%$ change; for $0.75 \%, 42 \%$; for $1 \%, 47 \%$; and for $2.5 \%$ (which is near the saturation point at this temperature) the change is $64 \%$.

Ethyl alcohol depresses the surface tension of water more than the same percentage of either methyl alcohol or acetic acid, which have pretty much the same effect, or of formic acid which causes a much smaller change.

It is impossible to represent any of these variations in surface tension with a change in concentration by a simple formula. For this reason all values observed are presented here. The curves for acetic acid and ethyl alcohol show points of inflection, as does also that for formic acid, to a slight degree. In the case of formic acid, from about $45 \%$ to $100 \%$ the curve is almost a straight line; for methyl alcohol, from $60 \%$ to $100 \%$, it is actually a straight line.

Duclaux ${ }^{1}$ has found that for aqueous solutions of homologous alcohols and acids the ratio of the percentage concentration of any two homologues,
${ }^{1}$ Ann. chim. phys., [5] 13, 76 (1878).
in the solutions exhibiting the same surface tension, is constant. This rulehas been tested by applying to it our values for the three alcohols, and the two acids. The result is fairly satisfactory, as will be observed from a glance at the following table, in which the results are taken from the plotted curves:

|  | $\mathrm{C}(\mathrm{MeOH})$ | C (EtOH) |  | C(Formic acid) |
| :---: | :---: | :---: | :---: | :---: |
| $\gamma$. | C(EtOH) | $\mathrm{C}(\mathrm{AmOH})$ | $\gamma$. | C (Acetic acid) |
| 46 | 1.95 | 18.3 | 51 | 3.18 |
| 48 | 1.98 | 18.3 | 55 | 3.13 |
| 50 | 2.01 | 18.9 | 56 | 3.08 |
| 52 | 2.04 | 18.9 | 57 | 3.05 |
| 54 | 2.08 | 18.9 | 59 | 3.05 |
| 56 | 2.10 | 18.9 | 61 | 3.06 |
| 58 | 2.11 | 19.0 | 63 | 3.04 |
| 60 | 2.11 | 19.0 | 64 | 3.05 |
| 62 | 2.13 | 18.9 | 65 | 3.05 |
| 64 | 2.10 | 18.9 | . | .... |

The agreement here, for the ratio of ethyl and amyl alcohols, is very good, but for the other combinations a trend in the results seems certain.

The restits for the pure liquids-ethyl alcohol, methyl alcohol, and acetic acid-differ slightly from those previously given by Morgan and MeAfee, and the discrepancy is not constant-which proves that on neither side could it be a question of a constant error. The water values; agreed perfectly in the two investigations. After examining a number of carefully purified samples of the liquids, it was concluded that these, slightly smaller, results are the correct ones, and that the fault probably lies in slight impurities present in the samples used in that previous work, where no such care in purification was thought necessary.

In addition to the results for the solutions at various temperatures given in the above tables, we have also calculated, for each solution, the values. of its Ramsay and Shields' constant, $k$ by aid of the equation

$$
k=\frac{\gamma_{1}\left(M / d_{1}\right)^{2 / 3}-\gamma_{2}\left(M / d_{2}\right)^{2 / 2}}{t_{1}-t_{2}}
$$

This was done to ascertain whether or not it would give any indication at all of the dis-association of the two associated constituents, as a result of the solution of the one in the other. This should be apparent if the theory to that effect of Jones and Lindsay ${ }^{2}$ is correct. It may be said here ${ }^{3}$ that the values of $k$ found for the solutions are invariably smaller than that of pure water or those of the other pure constituents; whereas, if the theory were true, and the Ramsay and Shields' constant could prover it to be so, the value of $k$ would be larger for the solution than the values;

[^2]for the pure constituents and approach more nearly the normal, nonassociated value of 2.12 . Whether it be the fault of the theory; or of the inability of the Ramsay and Shields' constant to show such a change, is, of course, impossible here to state, or even to theorize upon.

The average molecular weights here are found by dividing the weight of each constituent by its molecular weight as a gas. The summation of the two, then, will give the total number of mols present in solution in the known weight of the mixture. From this the average molecular weight of the substances present will be given by simple division. It might be mentioned here that Ramsay and Aston, in their work on mixtures of organic liquids, have followed a different method of calculation, for apparently they regard the average molecular weight of any mixed liquid, containing equal parts by weight, as simply the mean of the two constituent molecular weights, which is plainly incorrect.

## Summary.

The results of this investigation may be briefly summarized as follows:
I. The drop weights at $30^{\circ}$ of many concentrations each of aqueous solutions of ethyl, methyl, and amyl alcohols, and of acetic and formic acids have been determined. From them the values of the surface tension and of the capillary constant have been calculated.
2. The variation with the temperature of the surface tension and of the capillary constant, have also been found for certain selected concentrations of aqueous solutions of the compounds mentioned.
3. The very large effect of even minute amounts of amyl alcohol on the surface tension of water is shown-and attention is called to the fact that this might be made the basis of a very delicate method for the quantitative estimation of this substance in water.
4. The relationship of Duclaux-that, for aqueous solution of homologous alcohols and acids, the ratio of the concentrations of any two homologues in the solutions exhibiting the same surface tensions is constant -is confirmed.
5. Calculation of the Ramsay and Shields' constant for solutions of these associated liquids does not show it to approach the normal value, 2.12, more closely than the constituents themselves ${ }^{1}$-as it should if each of the associated liquids dis-associates the other, according to the theory advanced by Jones and Lindsay.
6. Associated liquids, when mixed, do not give for the mixture a surface tension equal to the mean of the two constituent surface tensions-which would seem to be a characteristic of the mixture of two non-associated liquids. On obtaining further evidence of this fact, it is possible that a new definition of normal molecular weight in the liquid state may result.

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${ }^{1}$ In fact, it is always smaller.


[^0]:    ${ }^{1}$ Ramsay and Aston, Z. physik. Chem., 15, 91, (1894).

[^1]:    ${ }^{1}$ This formic acid gave results when pure which checked the formula of Morgan and Stone (This Journal, 35, 1512) within $0.03 \%$, although the samples were of different origin and purified by different methods.
    ${ }^{2}$ For details of the standardization of a tip, see This Journal, 33, 1713-27 (I9II). All results in this paper are given in average to save space, although three or more determinations were always made of the weight of each number of drops, the agreement being within a few tenths of milligram on 25 drops.

    3 This Journal, 33, 1275-90 (igit).

[^2]:    ${ }^{1}$ This Journal, 33, 1275-90 (1911).
    ${ }^{2}$ Am. Chem. Jour., 28, 329 (1902).
    ${ }^{8}$ The results have not been included in the tables to save space.

